



Using @Risk for simulation modeling

Ashley Hill

Stochastic simulation model in Excel

- Each iteration:
 - Cells show random values drawn from probability distributions
 - Spreadsheet calculates outputs and results stored
- After many iterations:
 - Stored values for each output graphed, analyzed
 - Result represents *approximate* probability distribution of future outcomes

Monte Carlo simulation in spreadsheet models

- @RISK gives Excel the ability to allow certain quantities to be poorly known or variable
- 3 capabilities of @RISK:
 - Creating input distributions for uncertain quantities
 - Running a simulation
 - Analyzing results

@RISK functions

- @RISK functions take the format: =RiskXxx()
- 3 categories of @RISK functions:
 - **Distributions**:
 - RiskNormal(), RiskBinomial(), RiskTriang()
 - **Statistics** (allow reporting into Excel sheet):
 - RiskMean(), RiskCurrentIter(), RiskResultsGraph()
 - **Inputs** (which effect actions on input distributions)
 - RiskIndepc(), RiskCollect(), RiskTruncate()
- We will focus primarily on distributions



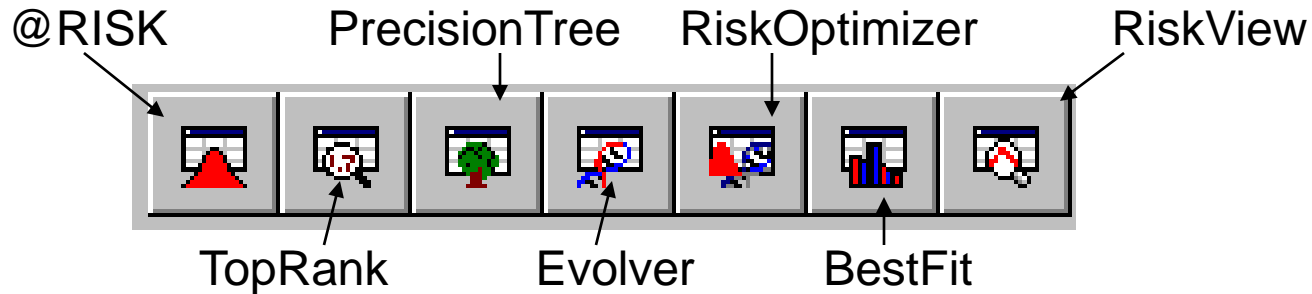
Introduction to @Risk

- Accessing @Risk in Excel
- Toolbars
- @Risk menus
- Model window
- Results window

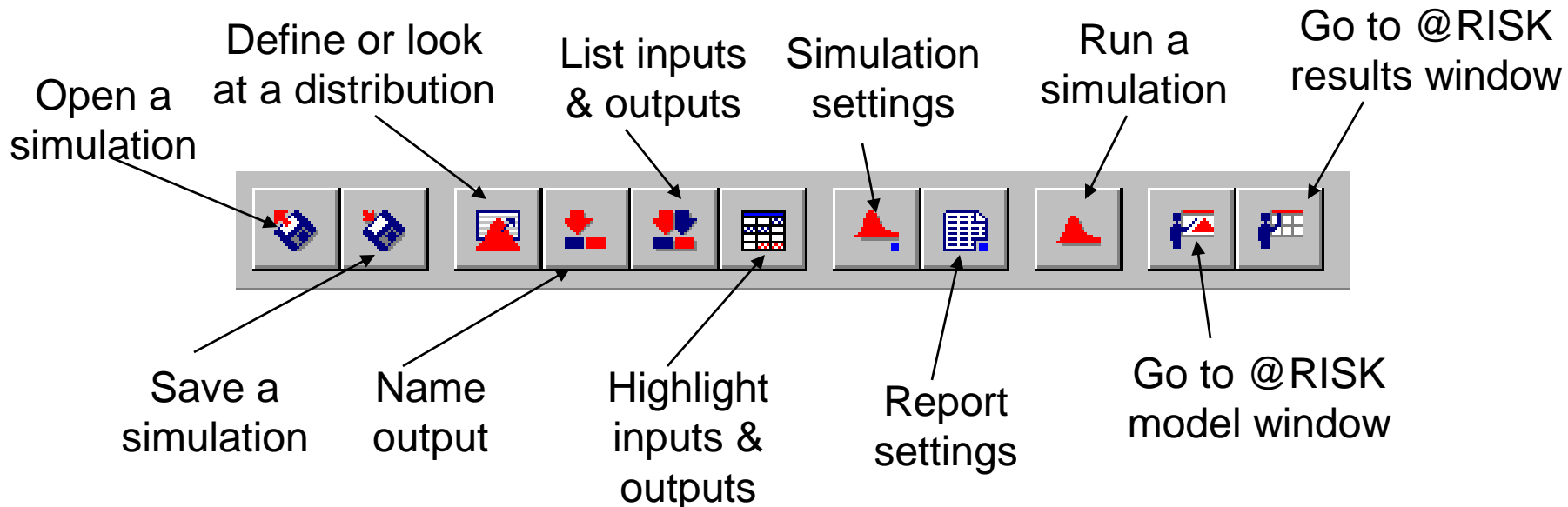
Working example

- We'll use Aaron's Reed-Frost example from this morning to explore @Risk
 - Population = 101
 - Initial number of susceptibles = 100
 - Initial number of cases = 1
 - $k \sim \text{Binomial}(4, 0.5)$

Palisade DecisionTools toolbar



@RISK toolbar





Menus

- File
- Edit
- View
- Insert
- Simulation
- Fitting/Results
- Graph
- Window
- Help



Model window

- List of inputs & outputs in current model
- Insert menu
- Distribution fitting (we will use in later example)



Results window

- List of inputs/outputs
- Summary statistics
- Insert menu
 - Detailed statistics
 - Data
 - Graph

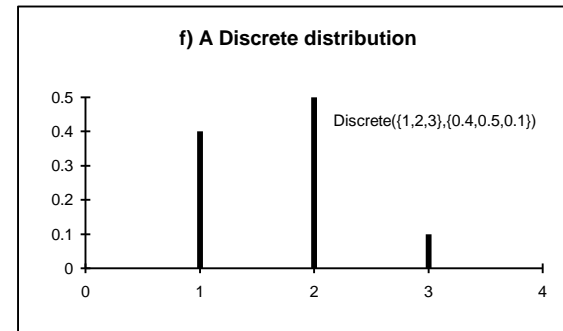
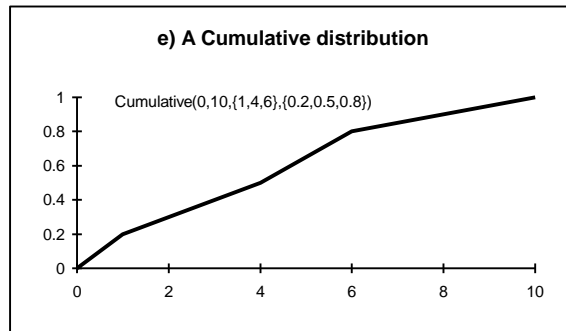
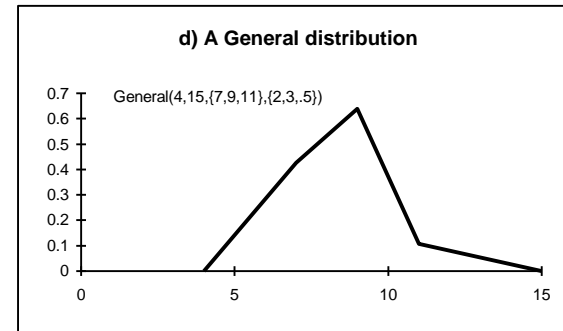
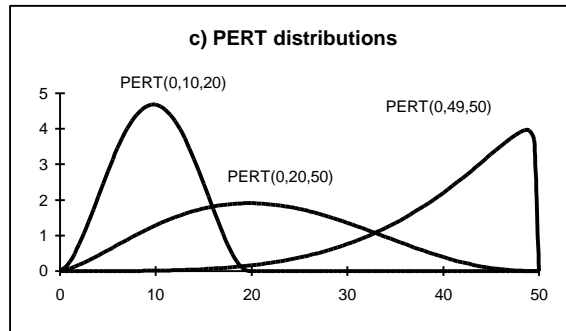
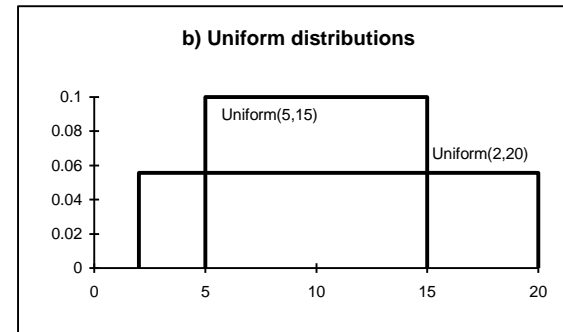
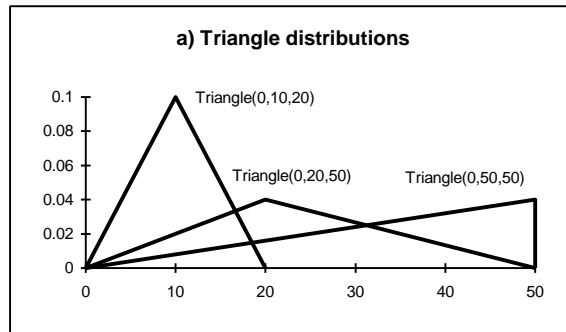


Creating input distributions

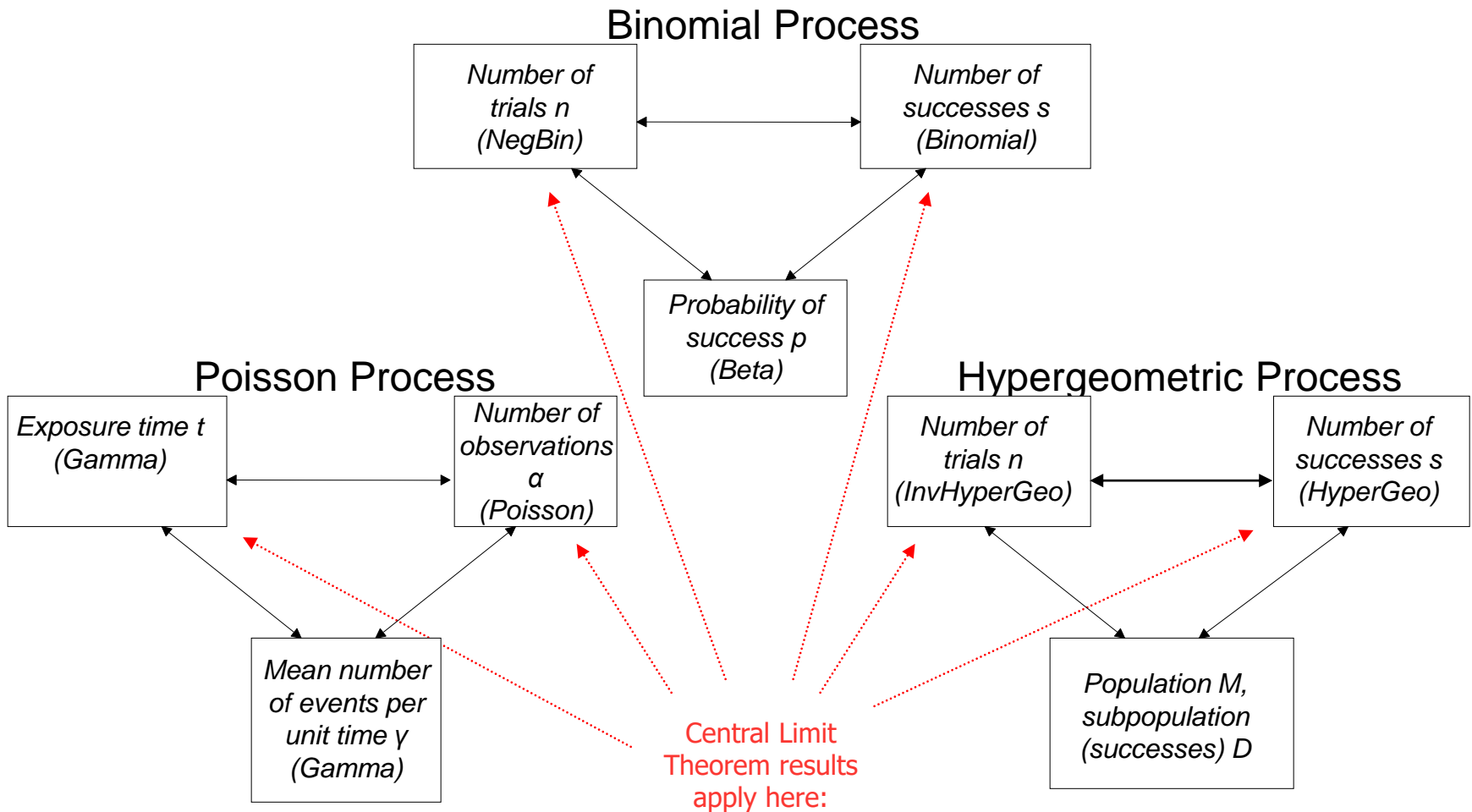
Review of probability distributions

- Parametric distributions:
 - Binomial Poisson Hypergeometric
 - Gamma NegBin Normal
- Empirical distributions (useful for data, expert opinion)
 - PERT Triangle Beta
 - General Discrete Uniform
 - Bootstrapping (sampling from existing data)
- Knowing which distribution to use requires working knowledge of probability theory

Review: Empirical probability distributions



Review: parametric distributions in 3 stochastic processes



Quick summary of some parametric distributions

Binomial process distributions	
Quantity	Formula
Number of successes	$s = \text{Binomial}(n, p)$
Probability of success	$p = \text{Beta}(s+1, n-s+1)$
Number of trials	$n = s + \text{NegBin}(s, p)$ (last trial is a success)
	$n = s + \text{NegBin}(s+1, p)$ (last trial is not known)
Poisson process distributions	
Number of events	$\alpha = \text{Poisson}(\lambda t)$
Mean number of events per unit exposure	$\lambda = \text{Gamma}(\alpha, 1/t)$
Time until first event	$t_1 = \text{Exponential}(1/\lambda)$
Time until first α events	$t_\alpha = \text{Gamma}(\alpha, 1/\lambda)$
Hypergeometric process distributions	
Number of successes (subpopulation) in sample	$s = \text{HyperGeo}(n, D, M)$
Number of samples to observe s successes	$n = s + \text{InvHyp}(s, D, M)$

Creating input distributions

- Select appropriate distribution
 - Fit distributions to data (if data available!)
 - Use distribution that is mathematically appropriate
 - Handy tools:
 - BetaBuster
 - Generates Beta parameters for expert opinion on Se, Sp, prevalence or other proportions
 - <http://www.epi.ucdavis.edu/diagnostictests/betabuster.html>

Example 1:

- In an adequate contact, the probability of transmitting Disease A from an infected to susceptible animal is 0.4.
 - A single infected animal has 40 adequate contacts with susceptible animals during its infectious period
 - On average, how many animals will an infected animal infect?
 - If 100 infected animals are released, what's the fewest number of new infections from one infected animal? What's the highest number of new infections per animal?

Example 1

- Working through the problem
 - What probability distribution to use?
 - What are the parameters for the distribution?
 - How many iterations should we run?
 - Insert distribution using @Risk
 - Run iterations
 - Evaluate output

Example 2

- We think that the probability of infection given adequate contact is 0.4, but when we asked experts, they said it was most likely 0.4, but was definitely less than 0.8
 - What parameter does this affect?
 - Is this uncertainty or variability?
 - How can we incorporate expert opinion into our model?

Example 3

- The average number of adequate contacts is 40, but anecdotally it ranges from 10 to 60 adequate contacts.
 - How does this change our results?
 - What distribution(s) could we use?
 - How do we add this to our simulation model?

Example 4

- A graduate student collected daily data on the number of adequate contacts between 40 animals.
 - How can we incorporate this data into our model?
 - Do we need any other information?
 - Fit a distribution
 - Bootstrap

Distribution fitting

- Distribution fitting

- Methods of comparison

- Visual

- Difference

- P-P and Q-Q

- Statistics and Goodness of Fit

- Statistics: Descriptives on data and distribution

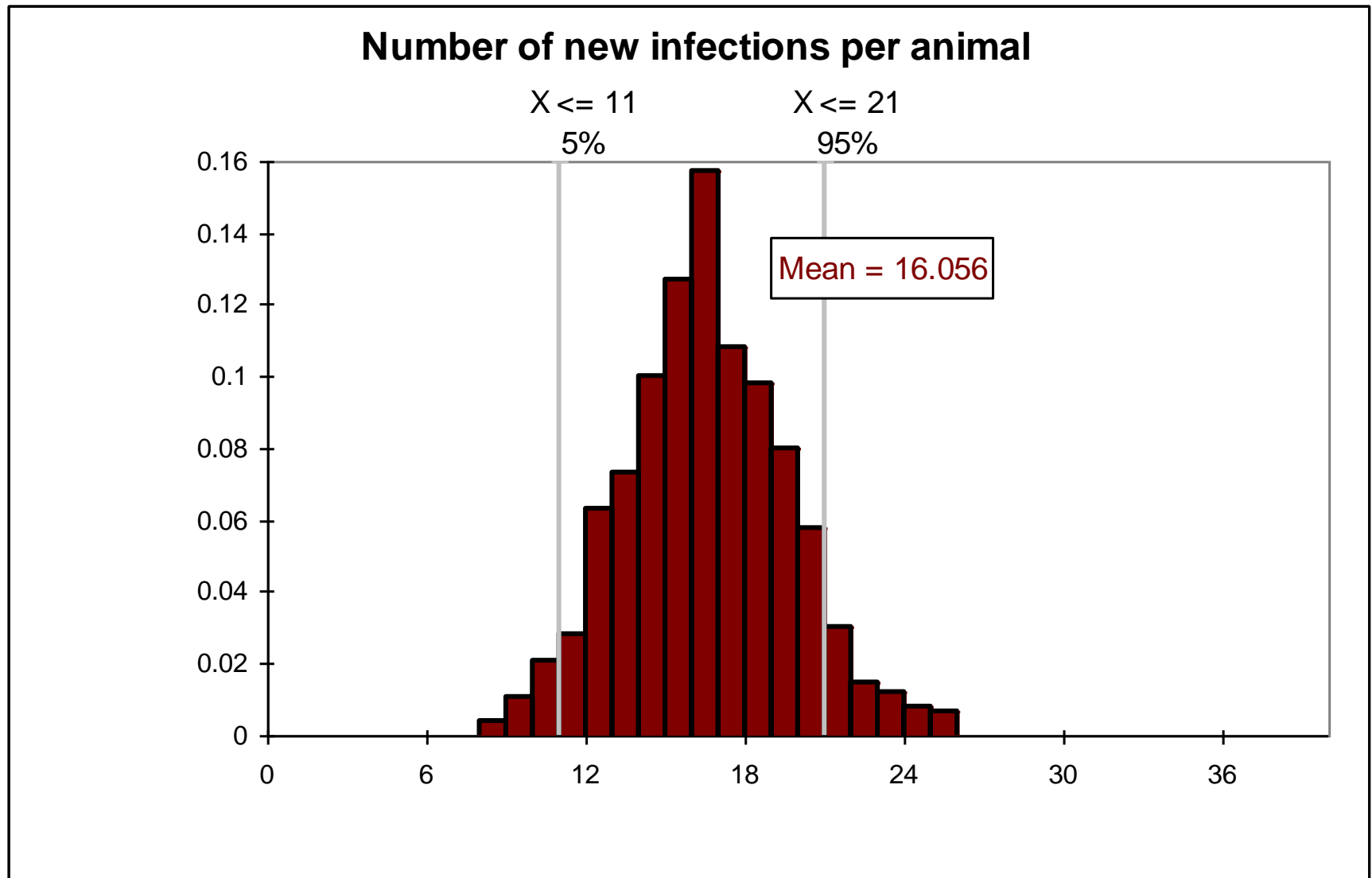
- GOF: Results of Chi-square, Anderson-Darling, and Kolmogorov-Smirnov testing



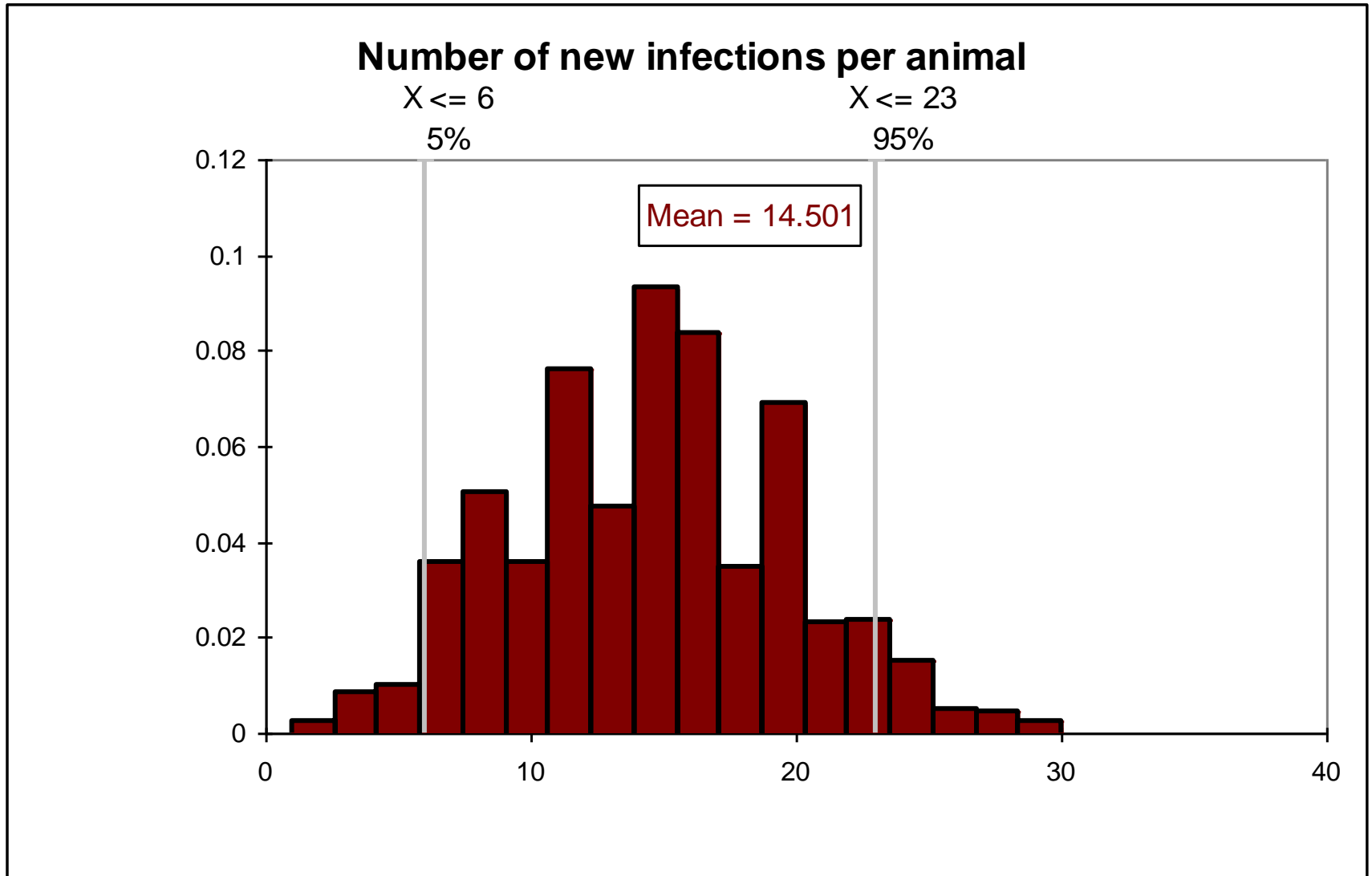
Comparing results

- Did incorporation of uncertainty about number of adequate contacts change our estimates of the numbers infected?

Constant number of adequate contacts (40)



Triangular distribution of adequate contacts (10,40,60)



Bootstrapped distribution of adequate contacts

