

*Preview of Tuesday:*  
**Introduction to  
stochastic modeling**

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# Today in review (I)

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- The epidemic model developed by Reed and Frost represents a class of mathematical models called chain binomial models
  - We have not yet discussed what a “chain binomial model” is
- The Reed-Frost model operates in discrete time units, where each time period is equal to the length of the average serial interval ( $\approx$  average incubation period) for the disease being modeled
- The number of cases in a particular time period can be calculated based on the number of cases from an earlier time period
- This calculation also uses the average number of adequate contacts (designated  $k$ ) that each individual has with others in the population during a single time period

# The Reed-Frost equation (more review)

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- $C_{t+1} = S_t(1 - q^{C_t})$

where:

$t$  indicates the time period

$C$  = # of cases (infectious individuals)

$S$  = # of susceptible individuals

$q$  = prob. of avoiding adequate contact

- $q = 1 - (\text{prob. of adequate contact}) = 1 - p$

- $p = k / (N - 1)$

where:

$k$  = average number of adequate contacts by an individual in a single time period

$N$  = size of the population

# Today in review (II)

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- Statistical tests, like the chi-square test or G test, can be used to assess the fit of results predicted by a model to actual outbreak data
- The goodness of fit of a model can be optimized by selecting an appropriate value for  $k$
- In the context of the basic Reed-Frost model,  $k$  is equivalent to  $R_0$

# Deterministic modeling

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- The Reed-Frost model, as constructed today, is a *deterministic* model
  - The model produces an estimate of the average number of new cases per time period
  - There is a closed form solution for the Reed-Frost function
  - There is no measure of variability or uncertainty connected with the result
- Real life is rarely so simple. For example...

# How many ways can you toss four coins?



*etc.*

- In four coin tosses, we expect that the most common result will be two heads
  - This would be the result of a deterministic model
- Two heads is not the only possible outcome: chance plays a role
  - A *stochastic* model will account for the role of chance

# Stochastic models

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- Stochasticity refers to the random or variable nature of events
- Characteristics of biological systems are often variable (usually within limits)
  - e.g., daily milk production
- When modeling disease, it is often useful to account for this natural variability
- Models may also include variability simply because little is known about a system

# Coming up tomorrow

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- We will continue to work with the Reed-Frost framework, incorporating variability or stochasticity into the basic model
- We will look at the benefits of stochastic modeling
- We will be introduced to some computational tools for creating stochastic models
- We will briefly examine a different approach to disease modeling, which will allow us to create much more complex models